Shiv Chhatrapati Shikshan Sanstha's

Rajarshi Shahu Mahavidyalaya, Latur

(Autonomous)



Structure and Curriculum of

Under Graduate Progr<mark>amme (II Y</mark>ear) of Science and Technology

B.Sc. in Mathematics

Approved by

Board of Studies

in

Mathematics Source

Rajarshi Shahu Mahavidyalaya, Latur

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w.e.f. June, 2024 (In Accordance with NEP-2020)

Review Statement

The NEP Cell reviewed the Curriculum of **B. Sc-II. Mathematics in UG** Programme to be effective from the **Academic Year 2024-25.** It was found that, the structure is as per the NEP-2020 guidelines of Govt. of Maharashtra.

Date: 13/03/2024

Place: Latur

NEP Cell Rajarshi Shahu Mahavidyalaya, Latur (Autonomous)

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CERTIFICATE

I hereby certify that the documents attached are the Bonafide copies of the Curriculum of **B. Sc.-II Mathematics** course to be effective from the **Academic Year 2024-25**.

Date: 13/03/2024 Place: Latur

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Dr. M S Wavare Chairperson Board of Studies in Mathematics Rajarshi Shahu Mahavidyalaya, Latur (Autonomous)

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ण संस्था

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(Autonomous) Members of Board of Studies in the Subject Mathematics Under the Faculty of Science and Technology

| Sr. No. | Name | Designation | In position |
|------------|--|-------------|-------------------------|
| 1 | Dr. Mahesh S Wavare | Chairperson | HoD |
| | Professor and Head, Department of | | |
| | Mathematics, Rajarshi Shahu 🥢 | | |
| | Mahavidyalaya, Latur (Autonomous) | | |
| 2 | Dr. Bhalchandra D. Karande | Member | V.C. Nominee |
| | Head and Associate Professor, Depart <mark>ment o</mark> f | | |
| | Mathematics, Maharashtra Udaygiri | | |
| | Mahavidyalaya, Udaygiri Dist. Latur. | | |
| 3 | Dr. S. D. Kendre, | Member | Academic Council |
| | Associate Professor, Department of | | Nominee |
| | Mathematics, | | |
| 4 | Dr. M.T. Conhono | Mombon | Acadamia Council |
| 4 | Associate Professor Department of | Member | Academic Council |
| | Mathematics | | Nommee |
| | Shivaji University, Kolhapur. | | |
| 5 | Dr. N. S. Darkunde | Member | Expert from outside for |
| | School of Mathematical Sci <mark>ences, S. R. T. M. U</mark> | | Special Course |
| | Nanded. | | • |
| 6 | Mr. S. S. Ranmal | Member | Expert from Industry |
| | Sungrace Computers Pvt Ltd, Pune. | | |
| 7 | Prof. S. M. Shinde | Member | P.G. Alumni |
| | Department of Mathematics, Government | | |
| | Amaravati | | |
| 8 | Dr. N. S. Pimple | Member | Faculty Member |
| 9 | Miss. S. D. Shinde | Member | Faculty Member |
| 10 | Mr. P. D. Bombalge | Member | Faculty Member |
| 11 | Mr. N. D. Kapale | Member | Faculty Member |
| 12 | Dr. A. A. Yadav | Member | Member from the same |
| | | | faculty |

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From the Desk of the Chairperson...

When Shiv Chhatrapati Shikshan Sanstha started the Science Faculty in Rajarshi Shahu Mahavidyalaya, Latur in 1971, the Department of Mathematics was founded. In the beginning, there was just one instructor for the PUC class and the first year of the B.Sc. B.Sc.-II and B.Sc. III year courses began in 1973 and 1974, respectively, in response to the natural expansion. During the 2017–2018 academic year, the department launched its M.Sc. Mathematics programme with a 30-student entry limit.

The undergraduate degree course in mathematics is a six- or eight-semester course spanned across three- or four-academic years, in accordance with the guidelines of the Undergraduate Curriculum Framework 2022 (UGCF 2022). The teaching and learning process is centered on the learner and includes both theoretical and practical elements. While guaranteeing that the student has a solid foundation in the topic and obtains in-depth knowledge, it provides flexibility in program structure. A student may choose courses from the syllabus that includes Discipline Specific Electives (DSEs), Generic Electives (GEs), Skill Enhancement Courses (SECs), Ability Enhancement Courses (AECs), and Value Addition Courses (VACs) in addition to the Discipline Specific Core (DSC) courses. As a result, the interdisciplinary approach and commitment to creative approaches within the curricular framework are highlighted.

The new National Education Policy (NEP), 2020, which includes significant elements, offers a platform to develop, nurture, grow, encourage, and multiply mathematical thinking. To achieve a balance between the requirement for employment in the twenty-first century and entrepreneurship, which is characterized by lateral, critical, and numerical thinking, the essential changes have been put in place. The NEP acknowledged the importance of mathematical thinking and how necessary it is for the country to become a Vishwa guru. The NEP provides children with the nutrition they require by making mathematics enjoyable and engaging from the very beginning. Because it encourages the development of computer skills and intuitive reasoning, the NEP also requires the adoption of a coding curriculum, which should start in middle school.

The courses for the UG Programme are framed using time tested and internationally popular text books so that the courses are at par with the courses offered by any other reputed universities around the world.

Only those concepts that can be introduced at the UG level are selected and instead of cramming the course with too many ideas the stress is given in doing the selected concepts rigorously. The idea is to make learning mathematics meaningful and an enjoyable activity rather than acquiring manipulative skills and reducing the whole thing an exercise in using thumb rules.

As learning Mathematics is doing Mathematics, to this end, some activities are prescribed to increase student's participation in learning. Duration of the degree Programme shall be six- or-eight semesters distributed in a period of three/four academic years.

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Dr. Mahesh S Wavare Chairperson Board of Studies in Mathematics

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Faculty of Science and Technology

Structure for Four Year Multidisciplinary Undergraduate Degree Programme in Mathematics Multiple Entry and Exit (In accordance with NEP-2020)

| Year | | Maj | or | | | VSC / | | | Credi | Cum. |
|----------------|---------|------------|----------|-----------------------|-----------------------|---------------|----------------------|----------------------|---------------|---------------------|
| & Leve l | Sem | DSC | DSE | Minor | GE/OE | SEC (VSEC) | AEC/ VEC | OJT,FP,CEP , RP | t per Sem. | /Cr. per exit |
| 1 | 2 | 3 | | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| | Ι | DSC V: | NA | DSM- I | <mark>GE-III</mark> : | SEC-III: | AEC-III: | CC-I: | 22 | |
| | | 04 Cr. | | 04 Cr | <mark>02 Cr.</mark> | 02 Cr. | Eng | 02 Cr.(SSC) | | |
| | | DSC VI: | | | | | 02 Cr. | Field | | |
| | | 04 Cr. | | | | | 1 | Project: | | |
| | | | | | | | | 02 Cr. | | 44 Cr. |
| | II | DSC | NA | D <mark>SM-</mark> II | G <mark>E-IV:</mark> | SEC-IV: | AEC-IV | CC-II: | 22 | UG |
| Ι | | VII: | | 0 <mark>4 Cr</mark> | <mark>02 Cr.</mark> | 02 Cr. | En <mark>g</mark> : | 02 Cr.(SSC) | | Certif |
| 4.5 | | 04 Cr. | | | | | <mark>02 C</mark> r. | Field | | icate |
| | | DSC | | | | | | Project: | | |
| | | VIII: | | | | | | <mark>0</mark> 2 Cr. | | |
| | | 04 Cr. | | | | | | | | |
| | | | | •• | | | | | | |
| | Cum | 16 | - | 08 | 04 | 02+02= | 02+02= | 08 | 44 | |
| | . Cr. | | | 11 | / | 04 | 04 | ती | | |
| Fvi | t Ontio | n. Award o | of UC Co | rtificate in | Major wit | h 11 Crodi | ts and Addi | tional 04 Cred | its Coro | NSOE |

Option: Award of UG Certificate in Major with 44 Credits and Additional 04 Credits Core NS Course/Internship or continue with Major and Minor

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Abbreviations:

- 1. DSC : Discipline Specific Core (Major)
- 2. DSE : Discipline Specific Elective (Major)
- 3. DSM : Discipline Specific Minor
- 4. GE/OE : Generic/Open Elective
- 5. VSEC : Vocational Skill and Skill Enhancement Course
- 6. VSC : Vocational Skill Courses
- 7. SEC : Skill Enhancement Course
- 8. AEC : Ability Enhancement Course
- 9. MIL : Modern Indian Lang<mark>uages</mark>
- 10. IKS : Indian Knowledge System
- 11. FSRCE : Fostering Social Responsibility & Community Engagement
- 12. VEC : Value Education Courses
- 13. OJT : On Job Training
- 14. FP : Field Projects
- 15. CEP : Community Engagement and Service
- 16. CC : Co-Curricular Courses
- 17. RP : Research Project/Dissertation
- 18. SES : Shahu Extension Services

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(Autonomous) Department of Mathematics B.Sc. -II Mathematics(Major and Minor)

| Year & Level | Semester | Course Code | Course Title | Credits | No. of Hrs. |
|-----------------|----------|--------------------------|-----------------------|---------|----------------|
| | | 201MAT3101 (DSC-V) | Real Analysis | 03 | 45 |
| | | 201MAT3103 | Lab Course-V | 01 | 30 |
| | | 201MAT31 <mark>02</mark> | Group Theory | 03 | 45 |
| | | (DSC-VI <mark>)</mark> | | | |
| | | 201MAT3 <mark>104</mark> | Lab Course-VI | 01 | 30 |
| | | 201MAT | Applied Mathematics | 03 | 45 |
| | 111 | (DSM-I) | | | |
| | | 201MAT | Lab Course-I(Minor) | 01 | 30 |
| | | GE-III | From Basket | 02 | 30 |
| | | (SEC-III) | From Basket | 02 | 30 |
| | | (AEC-III) | From Basket | 02 | 30 |
| | | CC-I | SSC | 02 | 30 |
| | | FP-I | Field Project-I | 02 | 60 |
| II | | 22 | | | |
| 5.0 | | 301MAT4101 | Ordinary Differential | 03 | 45 |
| | | (DSC-VII) | Equations | _ | |
| | | 301MAT4103 | Lab Course-VII | 01 | 30 |
| | | 301MAT4102 | Ring Theory | 03 | 45 |
| | | | | | 20 |
| | | 301MA14104 | | 01 | 30 |
| | IV | | Statistics | 03 | 45 |
| | | 201MAT | Lab Course-II (Minor) | 01 | 30 |
| | | GE-IV | From Basket | 02 | 30 |
| | | (SEC-IV) | From Basket | 02 | 30 |
| | | (AEC-IV) | From Basket | 02 | 30 |
| | | CC-II | SSC | 02 | 30 |
| | | FP-II | Field Project-II | 02 | 30 |
| | | Total Cred | lits | 22 | |
| | 44 | 1 | | | |



Rajarshi Shahu Mahavidyalaya, Latur (Autonomous)

| | Programme Outcomes (POs) for B.Sc. Programme |
|-----|---|
| P01 | Disciplinary Knowledge |
| | Comprehensive knowledge of science subjects which constitute |
| | the graduate programme and execution of scientific knowledge in |
| | the specific area. |
| P02 | Scientific Outlook |
| | The qualities of a scien <mark>ce gra</mark> duate such as observation, precision, |
| | analytical mind, logical <mark>thinkin</mark> g, clarity of thought and |
| | expression and system <mark>atic appro</mark> ach. |
| P03 | Self-Directed Life-long Learning |
| | Ability to appear for var <mark>ious competiti</mark> ve examinations or choose |
| | the post graduate progr <mark>amme or other r</mark> elated programme of |
| | their choice. |
| P04 | Research Skills |
| | Functional knowledge and applications of instrumentation and |
| | laboratory tech <mark>niques to do independent e</mark> xperime <mark>nts, interpret</mark> |
| | the results an <mark>d develop research ethos.</mark> |
| P05 | Problem Solving Skills |
| | Analytical and logical skills and critical thinking to extract |
| | information from qualitative and quantitative data, formulate |
| | and solve problems in a systematic and rational manner. |
| P06 | Professional Competence and Ethics |
| | Aptitude a <mark>nd ski</mark> lls to p <mark>erfor</mark> m the jobs in diverse fields such as |
| | science, en <mark>gine</mark> ering, i <mark>ndus</mark> tries <mark>, survey , education, b</mark> anking, |
| | development and planning, business, public service, self-business |
| | etc. with human rationale and moral values. |

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| Programme Specific Outcomes (PSOs) for B.Sc. in Mathematics | | | | | | | |
|---|---|--|--|--|--|--|--|
| | (Honors) | | | | | | |
| PSO No. | Upon completion of this Programme the students will be able to | | | | | | |
| PSO1 | To Develop their mathematical knowledge, oral, written, and practical | | | | | | |
| | skills in a way to enhance confidence and provide satisfaction. | | | | | | |
| PSO2 | To inculcate the confidenc <mark>e by</mark> developing a feel for numbers, patterns, | | | | | | |
| | and relationships. | | | | | | |
| PSO3 | To advance an ability t <mark>o cons</mark> ider, solve problems, present and interpret | | | | | | |
| | results. | | | | | | |
| PSO4 | To improve Communica <mark>tion and r</mark> eason using mathematical concepts. | | | | | | |
| PSO5 | To understand mathematical principles and their applications. | | | | | | |
| PSO6 | To foster the abilities to reason logically, to classify, to generalize and to | | | | | | |
| | prove. | | | | | | |
| PSO7 | To acquire the founda <mark>tion, appropriate</mark> to their further studies of | | | | | | |
| | mathematics an <mark>d</mark> of other disciplines. | | | | | | |
| PS08 | To qualify IIT <mark>-JA</mark> M a <mark>higher education e</mark> ntrance in the subject of | | | | | | |
| | Mathematics. | | | | | | |
| PSO9 | To do minor re <mark>search project in the field of Ma</mark> thematics. | | | | | | |
| PS010 | To nurture th <mark>e basic information of Indian Kno</mark> wledge System. | | | | | | |



Semester - III

शिव छत्रपती शिक्षण संस्था लातूर

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(Autonomous) Department of Mathematics

Course Type : DSC-VCourse Title : Real AnalysisCourse Code : 201MAT3101Credits : 03

Max. Marks: 75

Lectures: 45 Hrs.

Learning Objectives

LO1 To Understand Definition of Sequence and its properties

- LO2 To study Bolzano-Weierstrass theorem and Cauchy's criterion for convergence
- LO3 To study Sequence of functions
- LO4 To Study Infinite Series and Absolute Convergence

Course outcomes

- CO1 Know the definition of the limit of a sequence, evaluate the limits of a wide class of real sequences
- CO2 Do point wise and Uniform convergence
- CO3 Decide on convergence or divergence of a wide class of series
- CO4 Determine whether or not real series are convergent by comparison with standard series or using the Ratio Test
- CO5 Understand the concept of Absolute convergence and be familiar with the statements and some proofs of the standard results about Absolute convergence

| Unit | Title of Unit & Contents | Hrs. | | |
|------------|---|------|--|--|
| <u>NO.</u> | Sequences | 10 | | |
| - | 1 Introduction: Sequences and their limits | 10 | | |
| | 2 Limit theorems and Monotone Sequences | | | |
| | 3. Subsequences and Bolzano Weierstrass theorem | | | |
| | 4. The Cauchy's criterion. Properly divergent sequences | | | |
| | Unit Outcome: | | | |
| | U01 To acquire knowledge about convergent and divergent | | | |
| | Sequence. Charley Mahavidyalaya | | | |
| II | Sequence of functions | 12 | | |
| | 1. Pointwise and uniform convergence | | | |
| | 2. Interchange of limits | | | |
| | 3. The exponential and Logarithmic functions, The trigonometric | | | |
| | functions | | | |
| | Unit Outcomes: | | | |
| | U01 To study some special type of function | | | |
| | UO2 To check uniform convergence and pointwise convergence | | | |

| Unit No. | | Title of Unit & Contents | Hrs. |
|-------------|--------|---|------|
| III | Infini | te Series | 13 |
| | 1. | Introduction to series, infinite series, its convergence and sum | |
| | 2. | Cauchy general principle of convergence for series | |
| | 3. | General test for the convergence of positive term series | |
| | 4. | Comparison tests convergence of positive term series | |
| | 5. | D'alembert's ratio test, Cauchy nth root test , Raabe's test , | |
| | | Logarithmic test ,Cauchy Integral test , Cauchy condensation test, | |
| | | Abel's test | |
| | Unit (| Outcomes: | |
| | U01 | To study series of func <mark>tion.</mark> | |
| | U02 | To check convergent <mark>series</mark> and divergent series | |
| IV | Infini | te Series with positive and negative terms | 10 |
| | 1. | Absolute convergen <mark>ce Test f</mark> or Absolute convergence, Test for | |
| | | Non- absolute conve <mark>rgence</mark> | |
| | 2. | Conditional Converg <mark>ence</mark> | |
| | 3. | Alternating series, Le <mark>ibnitz's Theor</mark> em | |
| | 4. | Radius of Convergenc <mark>e</mark> | |
| | Unit (| Outcomes: | |
| | U01 | To calculate the radius of convergence | |

- 1. Robert G.Bartle & Donald R Sherbert , "Introduction to real Analysis" (Third Edition) (Wiley Student Edition)
- 2. George B. Thomas, Ross L. Finney, "Calculus and Analytical Geometry" (Sixth Edition) (Narosa Publishing House)
- 3. Robert Wrede & Murray R, "Advanced Calculus" (Third Edition) Spiegel
- 4. S.C.Malik & Savita Arora, "Mathematical Analysis" New age International Ltd.
- 5. Shanti Narayan M. D. Raisinghaniya ,"Elements of Real Analysis", (S.Chand & Comp. Ltd.)
- 6. S.K.Mapa , "Introduction to real Analysis" (Sixth Edition)
- 7. Richard Goldberg , " Methods of Real Analysis", John Wiley & Sons, Inc. New york



(Autonomous) Department of Mathematics

Course Type : DSC-VCourse Title : Lab Course (Based on DSC-V)Course Code : 201MAT3103Credits : 01Max. Marks: 50

Hours: 30

Learning Objectives

- LO1 To Understand definition of Sequence and its properties
- LO2 To study Bolzano-Weierstrass theorem and Cauchy's criterion for convergence
- LO3 To study Sequence of functions
- LO4 To Study Infinite Series and Absolute Convergence

Course outcomes

- CO1 Know the definition of the limit of a sequence, evaluate the limits of a wide class of real sequences;
- CO2 Do point wise and Uniform convergence
- CO3 Decide on convergence or divergence of a wide class of series;
- CO4 Determine whether or not real series are convergent by comparison with standard series or using the Ratio Test;
- CO5 Understand the concept of Absolute convergence and be familiar with the statements and some proofs of the standard results about Absolute convergence

| Deve et la el | IL.'t |
|---------------|--|
| Practical | Unit |
| No. | |
| 1 | Using the definition of the limit of a sequence to establish the |
| | following limits. $(2n)$ |
| | a) $\lim \left(\frac{n}{n^2+1}\right) = 0$ c) $\lim \left(\frac{2n}{n+1}\right) = 2$ |
| Ra | b) $\lim_{n \to \infty} \left(\frac{3n+1}{2n+5}\right) = \frac{3}{2}$ and view $\lim_{n \to \infty} \left(\frac{n^2-1}{2n^2+3}\right) = \frac{1}{2}$ |
| 2 | Show that: |

| 11 | Show that $\lim_{n \to \infty} \left(\frac{nx}{1 + nx} \right) = 0$, for all x in R, $x \ge 0$. |
|----|--|
| 12 | Let $f: \mathfrak{R} \to \mathfrak{R}$ be uniformly continuous on \mathfrak{R} and let |
| | $f_n(x) = f(x+1/n) \text{ for } x \in \Re \text{ .Show that } (f_n) \text{ converges uniformly on } \Re \text{ to } f$ |
| 13 | The exponential function satisfies the following properties: |
| | i) $E(x) \neq 0$ for all $x \in R$ |
| | ii) $E(x+y) = E(x)E(y)$ for all $x, y \in R$; |
| | $iii) E(r) = e^r for \ all \ r \in Q$ |
| 14 | Calculate cos(.2),sin(.2) and cos 1,sin 1 correct to four decimal places. |
| 15 | Show that $ \sin x \le 1$ and $ \cos x \le 1$ for all $x \in R$. |
| 16 | Show that if $0 \le x \le a$ and $n \in N$, then |
| | $1 + \frac{x}{1!} + \dots + \frac{x^n}{n!} \le e^x \le 1 + \frac{x}{1!} + \dots + \frac{x^{n-1}}{(n-1)!} + \frac{e^a x^n}{n!}$ |
| 17 | Does the series $\sum_{n=1}^{\infty} \left(\frac{\sqrt{n+1} - \sqrt{n}}{\sqrt{n}} \right) convegre?$ |
| 18 | Does the series $\sum_{n=1}^{\infty} \left(\frac{\sqrt{n+1} - \sqrt{n}}{n} \right)$ convegre ? |
| 19 | Show that the series $\frac{1}{1^2} + \frac{1}{2^3} + \frac{1}{3^2} + \frac{1}{4^3} + \dots$ is convergent, but both the ratio and the Boot Tests fail to apply |
| 20 | If a and b are positive numbers, then $\sum (an+b)^{-p}$ converges if $p > 1$ and |
| 21 | diverges if $P \ge 1$. |
| 41 | Show that the series $1 + \frac{1}{2} - \frac{1}{3} + \frac{1}{4} + \frac{1}{5} - \frac{1}{6} + + - \dots$ is divergent |
| 22 | Test the following series for convergence and for absolute convergence. |
| | i) $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^2+1}$ if $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n+1}$ |
| | iii) $\sum_{n=1}^{\infty} \frac{(-1)^{n+1}n}{n+2}$ |
| | |

| 23 | Discuss the series whose nth term is: |
|----|--|
| | i) $(-1)^n \frac{(n)^n}{(n+1)^{n+1}}$ ii) $\frac{(n)^n}{(n+1)^{n+1}}$ |
| 24 | Determine the radius of convergence of the series $\sum a_n x^n$, where a_n is given by : |
| | i) $1/n^n$ ii) $\frac{n^{\alpha}}{n!}$ |

- 1. Robert G.Bartle & Donald R Sherbert , "Introduction to real Analysis" (Third Edition) (Wiley Student Edition)
- 2. George B. Thomas, Ross L. Finney, "Calculus and Analytical Geometry" (Sixth Edition) (Narosa Publishing House)
- 3. Robert Wrede & Murray R, "Advanced Calculus" (Third Edition) Spiegel
- 4. S.C.Malik & Savita Arora, "Mathematical Analysis" New age International Ltd.
- 5. Shanti Narayan M. D. Raisinghaniya ,"Elements of Real Analysis", (S.Chand & Comp. Ltd.)
- 6. S.K.Mapa ,"Introduction to real Analysis" (Sixth Edition)
- 7. Richard Goldberg , " Methods of Real Analysis", John Wiley & Sons, Inc. New york





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Department of Mathematics

Course Type : DSC-VICourse Title : Group TheoryCourse Code : 201MAT3102Credits : 03

Max. Marks: 75

Lectures: 45 Hrs.

Learning Objectives:

- LO1 To study basic group theory.
- LO2 To study Subgroups, Normal Subgroup, Quotient Group, Homomorphism, Isomorphism.
- LO3 To study Cayley and Lagrange theorem
- LO4 To discuss about external direct product and normal subgroup

Course Outcomes:

- CO1 Categorize group structures
- CO2 Find quotient group, subgroups of a given group.
- CO3 Analyze group structure from its order.
- CO4 Study isomorphic group and compute new group of order n.

| Unit No | | Title of Unit & Contents | Hrs. |
|------------|--------|--|------|
| I | Grou | os and Subgroup | 11 |
| | 1. | Definition of group, subgroups. | |
| | 2. | Elementary properties of groups, finite groups. | |
| | 3. | Cyclic groups and its properties. | |
| | Unit (| Dutcomes: | |
| | U01 | Acquaint with the b <mark>asic concepts of group and its exam</mark> ples. | |
| | U02 | Able to find structures of different groups. | |
| II | Perm | utation groups and Isomorphism | 11 |
| | 1. | Symm <mark>etric gro</mark> ups, P <mark>ermut</mark> ations | |
| | 2. | Group i <mark>somo</mark> rphism | |
| | 3. | Automorphism and their properties, Cayley's theorem | |
| | Unit (| Dutcome: | |
| | U01 | Can relate isomorphism of groups. | |
| III | Coset | and Lagrange's theorem | 11 |
| | 1. | Definition of coset and properties | |
| | 2. | Lagrange's theorem and its consequences | |
| | 3. | An application of cosets to permutation groups. | |
| | Unit (| Dutcomes: hi Shahu Mahavidyalaya | |
| | U01 | Can find different cosets of a group. | |
| IV | Direc | t Product | 12 |
| | 1. | External direct product | |
| | 2. | Definition and examples of normal subgroups and factor groups. | |
| | Unit (| Outcomes: | |
| | U01 | One can Apply external direct product to obtain new groups. | |

- 1. Joseph A. Gallian, "Contemporary Abstract Algebra", (Fourth Ed.), Narosa Publication, 1999.
- 2. J.B. Fraleigh, "A first Course in Abstract Algebra", Narosa Publication.
- 3. I. N. Herstein, "Topics in Algebra", Second Edition.
- V.K. Khanna, S.K. Bhambri, "A Course in Abstract Algebra", Vikas Publishing House.
 (Second Edition)
- 5. David Dummit and Richard Foote, "Abstract Algebra", John Wiley and Sons
- 6. P. B. Bhattacharya, S. K. Jain and S. R. Nagpaul, "Basic Abstract Algebra", (Second Ed.), Cambridge Univ. Press (Indian Ed.1995)





(Autonomous) Department of Mathematics

Course Type : DSC-VICourse Title : Lab Course (Based on DSC-VI)Course Code : 201MAT3104Credits : 01Max. Marks: 50

Hours: 30

Learning Objectives:

- LO1 To study basic group theory.
- LO2 To study Subgroups, Normal Subgroup, Quotient Group, Homomorphism, Isomorphism.
- LO3 To study Cayley and Lagrange theorem.
- LO4 To discuss about external direct product and normal subgroup

Course Outcomes:

- CO1 Categorize group structures
- CO2 Find quotient group, subgroups of a given group.
- CO3 Analyze group structure from its order.
- CO4 Study isomorphic group and compute new group of order n.

| Practical | Practical |
|-----------|--|
| NO. | |
| 1 | Prove that the set $GL(2,R) = \left\{ \frac{[a \ b \ c \ a]}{a,b,c,d \in R, ad-bc\neq 0} \right\}$ of 2 × 2 matices with |
| | real e <mark>ntries an</mark> d non- <mark>zero d</mark> eterminant is non_abelian group under the |
| | operation of matrix multiplication? |
| 2 | Show that the set {5,15 ,25,35} is a group under multiplication modulo |
| | 40. What is identity of this group? Can you see any relation between? |
| 3 | Find the inverse of the element $[2 6 3 5]$ in GL(2, \mathbb{Z}_{11}) |
| 4 | Prove that a group G is abelian if and only if (ab) ⁻¹ =a ⁻¹ b ⁻¹ for all a,b in G |
| 5 | Construct Cayley table for U(12) |
| 6 | Find all subgroups of D ₃ and find how many subgroups of order does D ₃ ? |
| 7 | In the group ℤ find |
| | i. <{8,4}> |
| | ii. <{8,15}> |
| | iii. <{6,15}> |
| | iv. <{m,,n}> |

| Practical | Practical |
|-----------|---|
| No. | |
| | v. <{12,18,45}> |
| 8 | Let R^* be the group of nonzero real numbers under multiplication and let |
| | H= $\left\{\frac{x \in R^*}{r^2 \text{ is rational}}\right\}$ prove that H is subgroup of R^* . Can the exponent 2 be |
| | replaced by any positive integer and still have H be a group? |
| 9 | Find all generators of \mathbb{Z}_6 , \mathbb{Z}_8 , \mathbb{Z}_{30} . |
| 10 | Determine the number of cyclic groups of order 4 in D _n |
| 11 | How many elements of order 5 are their in A ₆ |
| 12 | Determine all possible order of elements of S ₇ . |
| 13 | Show that number of c <mark>yclic group</mark> of order n upto isomorphism is 1. Hence |
| | find number of groups <mark>of order p up</mark> to isomorphism for any prime p. |
| 14 | Let G be a group. Prove that the mapping $a(g)=g^{-1} \forall g \in G$ is automorphism iff |
| | G is abelian. |
| 15 | Show that \mathbb{Z} has infinitely many subgroup isomorphic to \mathbb{Z} |
| 16 | Show that the mapping from U(16) to itself given by $x \rightarrow x^3$ is an automorphism. |
| 4.7 | What about $x \rightarrow x^5$ and $x \rightarrow x^7$? Generalize |
| 17 | Discuss the group of symmetries of an equilateral triangle |
| 18 | Discuss the group of symmetries of a square |
| 19 | Comment on converse of Lagrange's Theorem. |
| 20 | Sh <mark>ow that orde</mark> r of pr <mark>oper subgroup</mark> of a group of order 75 can be at most 75 |
| 21 | Let $ G = 15$. If G has only one subgroup of order 3 and only one subgroup of |
| | order 5 then prove that G is cyclic group. Generalize to $ G = pq$. Where p |
| | and q are prime |
| 22 | Find the number of elements of order 5 in $\mathbb{Z}_{25} \oplus \mathbb{Z}_5$. |
| 22 | Prove or disprove that |
| 23 | $2 \mathbb{Z} \oplus \mathbb{Z}$ is cyclic |
| | h. $\mathbb{Z}_2 \oplus \mathbb{Z}_3$ is cyclic |
| | C. $\mathbb{Z}_4 \oplus \mathbb{Z}_6$ is cyclic b a burn whether a barried value |
| | Rajos strandi inaliaviu yalaya, |
| 24 | Prove that every subgroup H of a Group G such that $[G: H] = 2$ is normal. |
| | hence $\frac{G}{H}$. |

- 1. Joseph A. Gallian, "Contemporary Abstract Algebra", (Fourth Ed.), Narosa Publication, 1999.
- 2. J.B. Fraleigh, "A first Course in Abstract Algebra", Narosa Publication.
- 3. I. N. Herstein, "Topics in Algebra", Second Edition.
- 4. V.K. Khanna, S.K. Bhambri, "A Course in Abstract Algebra", Vikas Publishing House. (Second Edition)
- 5. David Dummit and Richard Foote, "Abstract Algebra", John Wiley and Sons
- 6. P. B. Bhattacharya, S. K. Jain and S. R. Nagpaul, "Basic Abstract Algebra", (Second Ed.), Cambridge Univ. Press (Indian Ed.1995)





(Autonomous) Department of Mathematics

Course Type : DSM-ICourse Title : Applied MathematicsCourse Code : 201MAT3301Credits : 03 M

Max. Marks: 75

Lectures: 45 Hrs.

Learning Objectives:

- LO1 To study set theory and Functions
- LO2 To study basic trigonometry
- LO3 To learn basic calculus
- LO4 To familiarize with derivative and integration

Course Outcomes:

- CO1 Solve real-life problems requiring interpretation and comparison of complex numeric summaries which extend beyond simple measures of center.
- CO2 Solve a system of equations containing one first-degree polynomial and one seconddegree Polynomial
- CO3 Apply various concepts of right triangle trigonometry
- CO4 Relate the tangent and area problems to differential and integral calculus.

| Unit | Title of Unit & Contents | |
|------|--|----|
| No. | | |
| I | Elementary Algebra | 12 |
| | 1. Sets; R <mark>elation</mark> s and Functions | |
| | 2. Mathematical Induction; Logarithms | |
| | 3. Complex numbers | |
| | 4. Linear and Quadratic equations | |
| | Unit Outcome: | |
| | U01 To solve problems using logarithm tool | |
| | UO2 To know various types of methods to solve linear and quadratic | |
| | equations. | |
| II | Trigonometry and Geometry | 12 |
| | 1. Trigonometry and a wantavic yaidya. | |
| | 2. Cartesian System of Rectangular Coordinates | |
| | 3. Straight lines and Family | |
| | 4. Three Dimensional Geometry | |
| | Unit Outcome: | |
| | U01 To understand basic trigonometric functions. | |
| | UO2 To familiarize with the three dimensional geometry | |
| III | Elementary Calculus | 08 |
| | 1. Sequences and Series | |

| Unit | Title of Unit & Contents | | Hrs. |
|------|--------------------------|---|------|
| INO. | 2 | Matrices and Data and a | |
| | 2. | Matrices and Determinants | |
| | 3. | Boolean Algebra | |
| | 4. | Limits and Continuity | |
| | Unit | Outcome: | |
| | U01 | To find inverse of matrices | |
| | U02 | To understand the concept of Limit and continuity | |
| IV | Deriv | vative and Integration | 13 |
| | 1. | Differentiation; Ordinary Differential Equations Application of | |
| | | Derivatives | |
| | 2. | Integration as inverse process of differentiation | |
| | 3. | Definite and indefinit <mark>e inte</mark> grals | |
| | 4. | Methods of Integration | |
| | 5. | Integration by parts. | |
| | Unit | Outcome: | |
| | U I I I U | | |

- 1. S. K. Goyal, "Objective Mathematics", Arihant Prakashan, Meerut
- 2. V. Venkateshwara Rao, N. Krishnamurthy, B.V.S.S. Sarma, "Intermediate Mathematics", Vol-I, S. Chand & Company, New Delhi.
- 3. Dorai Raj, " Business Mathematics", Sahitya Bhawan, Agra.
- 4. S. Saha, "Basic Business Mathematics and Statistics", New Central Book Agency(P), Ltd, Calcutta.





(Autonomous) **Department of Mathematics**

Course Type : DSM-I Course Title : Lab Course (Based on DSM-I) Course Code: 201MAT3302 Credits :01 Max. Marks: 50 _____

Lectures: 30 Hrs.

Learning Objectives:

L01 To study set theory and Functions

L02 To study basic trigonometry

L03 To learn basic calculus

L04 To familiarize with derivative and integration

Course Outcomes:

- C01 Solve real-life problems requiring interpretation and comparison of complex numeric summaries which extend beyond simple measures of center.
- CO2 Solve a system of equations containing one first-degree polynomial and one seconddegree Polynomial
- CO3 Apply various concepts of right triangle trigonometry
- C04 Relate the tangent and area problems to differential and integral calculus

| Practical No. | Practical's |
|---------------|--|
| 1 | Pro <mark>blems on Se</mark> ts; Re <mark>lations and F</mark> unctions |
| 2 | Problems on Mathematical Induction |
| 3 | Proble <mark>ms on</mark> Logarit <mark>hms</mark> |
| 4 | Problem <mark>s o</mark> n Compl <mark>ex nu</mark> mbers et al set and set and |
| 5 | Problems on Linea <mark>r an</mark> d Quadratic equations |
| 6 | Problems on Trigonometry |
| 7 | Problems on Cartesian System of Rectangular Coordinates |
| 8 | Problems on Straight lines and Family |
| 9 | Problems on Three Dimensional Geometry |
| 10 | Problems on Sequences and Series |
| 11 | Problems on Matrices and Determinants |
| 12 | Problems on Boolean Algebra |
| 13 | Problems on Limits and Continuity |
| 14 | Problems on Differentiation |
| 15 | Problems on Ordinary Differential Equations |
| 16 | Problems on Application of Derivatives |
| 17 | Problems on Integration as inverse process of differentiation |

| 18 | Problems on Definite and indefinite integrals |
|----|---|
| 19 | Problems on Methods of Integration |
| 20 | Problems on Integration by parts |

- 1. S. K. Goyal, "Objective Mathematics", Arihant Prakashan, Meerut
- V. Venkateshwara Rao, N. Krishnamurthy, B.V.S.S. Sarma, "Intermediate Mathematics", Vol-I, S. Chand &Company, New Delhi.
- 3. Dorai Raj, "Business Mathematics", Sahitya Bhawan, Agra.
- 4. S. Saha, "Basic Business Mathematics and Statistics", New Central Book Agency(P), Ltd, Calcutta.



Semester - IV



।। आरोह तमसो ज्योतिः।।



(Autonomous) Department of Mathematics

Course Type : DSC-VIICourse Title : Ordinary Differential EquationCourse Code : 201MAT4101Credits : 03Max. Marks: 75Lectures: 45 Hrs.

Learning Objectives:

- LO1 Learn to solve ODEs.
- LO2 Learn to solve first-order linear ODEs using various methods (separation of variables, integrating factor, etc.).
- LO3 Learn to solve systems of first-order linear ODEs
- LO4 Learn to solve a second-order differential equation with constant coefficients and variable coefficients.

Course Outcomes:

- CO1 Obtain general solutions to first-order, second-order, and higher-order homogeneous and non-homogeneous differential equations by manual and technology-based methods.
- CO2 Identify and apply initial and boundary values to find particular solutions to firstorder, second-order, and higher order homogeneous and non-homogeneous differential equations by manual and technology-based methods, and analyze and interpret the results.
- CO3 Select and apply appropriate methods to solve differential equations; these methods will include, but are not limited to, undetermined coefficients, variation of parameters.
- CO4 Solve ordinary differential equation more than two variable.

| Unit No. | Title of Unit & Contents | Hrs | | | |
|-------------|---|-----|--|--|--|
| Ι | Definitions and Formation of Differential Equation | | | | |
| | 1. Preliminaries: Ordinary and partial differential equations order and degree. | | | | |
| | 2. Solutions and constants of integration. | | | | |
| | 3. The derivation of differential equation. Solutions, general, particular, singular. | | | | |

| Unit No. | Title of Unit & Contents | Hrs |
|-------------|--|---------|
| | 4. Geometrical meaning of differential equation of the first order ar | d |
| | degree. | |
| | Unit Outcomes: | |
| | UO1 Identify the order and degree of a differential equation. | |
| | UO2 Differentiate between general, particular, singular. solutions of | |
| | differential equations. | 10 |
| II | Equations of the First order and of the First Degree | 12 |
| | 1. Equation of the form $f_1(x)dx+f_2(y)dy=0$. | |
| | 2. Equations homogeneous in x and y. | |
| | 3. Non-homogeneous equation of the first degree in x and y. | -+ |
| | 4. Exact differential equations: condition that an equation of the fir | st |
| | Order be exact. | |
| | 5. Rules for finding the solution of an exact differential equation | n, W |
| | and V | v |
| | 6 Linear equations equations reducible to the linear form | |
| | Unit Outcomes. | |
| | IIO1 Develop critical thinking skills to analyze and choose appropria | te |
| | methods for solving different types of first-order and first-degra | |
| | equations | |
| | UO2 Differentiate between linear and nonlinear equations | |
| III | Linear Differential equations with constant coefficient | 12 |
| | 1. Linear equations. The complementary function, the particula | ar |
| | Integral, the complete integral. | |
| | 2. The linear equation with constant coefficient and second member | er |
| | zero. Case of the auxiliary equation having equal roots, imaginat | v |
| | roots, the symbol D, theorem concerning D. | |
| | 3. The linear equation with constant coefficient and second member | er |
| | is a function of x, the symbolic function $1/f(D)$, Method of finding | ıg |
| | the Particular integral. | 0 |
| | 4. Trajectories, determination of orthogonal trajectories in Cartesia | in |
| | and polar coordinates, working rule, self-orthogonal trajectories | 5. |
| | Unit Outcomes: | |
| | UO1 Define linear differential equations with variable coefficients. | |
| | UO2 Differentiate between linear and nonlinear differential equation | s. |
| IV | Linear Differential equations with variable coefficients | 15 |
| | 1. The Homogeneous linear equation. First method of solution | |
| | 2. Second method of Solution: To find the a) complementation | ту – |
| | function, b) particular integral. | |
| | 3. The symbolic functions f (θ) and 1/f(θ), method for finding | ıg |
| | particular integral. | |
| | 4. Integral corresponding to a term of form x^m in the second | ıd |
| | member, equations reducible to the homogeneous linear form. | |
| | 5. Equation of the second order, the complete solution in terms | of |
| | a known integral, relation between the integrals, solution between the |)y |
| | inspection by means of first two integrals by variation | of |
| | inspection, by means of mist two integrals, by variation | |

| Unit No. | | Title of Unit & Contents | Hrs |
|-------------|---------------|--|-----|
| | 6. | Ordinary differential equation with more than two variables: Simultaneous linear differential equation and their solutions. Geometrical meaning, single differential equation that are integrable, method of finding the solution of the single integrable equation. | |
| | Unit Outcome: | | |
| | U01 | To provide a comprehensive understanding of linear differential equations with variable coefficients | |

- 1. Daniel A. Murray, "Introductory Course in Differential Equations", Universities Press
- 2. G. F. Simmons "Differential Equations with Applications and Historical Notes", Second Edition, Mc Graw Hill.
- 3. M.D. Raisinghania, "Ordinary and Partial Differential Equations", S Chand and Company Ltd
- 4. T M Karade, "Differential Equation", Sonu –Nilu Publication





(Autonomous) Department of Mathematics

Course Type : Lab Course – VIICourse Title : Lab Course (Based on DSC-VII)Course Code : 201MAT4103Credits : 01Max. Marks: 50Lectures: 30 Hrs.

Learning Objectives:

- LO1 Learn to solve ODEs.
- LO2 Learn to solve first-order linear ODEs using various methods (separation of variables, integrating factor, etc.).
- LO3 Learn to solve systems of first-order linear ODEs
- LO4 Learn to solve a second-order differential equation with constant coefficients and variable coefficients.

Course Outcomes:

- CO1 Obtain general solutions to first-order, second-order, and higher-order homogeneous and non-homogeneous differential equations by manual and technology-based methods.
- CO2 Identify and apply initial and boundary values to find particular solutions to firstorder, second-order, and higher order homogeneous and non-homogeneous differential equations by manual and technology-based methods, and analyze and interpret the results.
- CO3 Select and apply appropriate methods to solve differential equations; these methods will include, but are not limited to, undetermined coefficients, variation of parameters.
- CO3 Solve ordinary differential equation more than two variable.

| Practical No. | Unit |
|---------------|---|
| 1 | 1. Derive the differential equation $(x-a)^2+(y-b)^2=r^3$ |
| 2 | Find the differential equation of all circles which pass through the origin and whose centre are on x-axis. |
| 3 | Solve 3ex tany dx + (1-e ^x) sec ² y dy=0. |
| 4 | Solve $(4x+3x)\frac{dy}{dx} + y - 2x = 0$ |

| Practical No. | Unit |
|---------------|--|
| 5 | Solve (2ax+by+g)dx+(2cy+bx+e)dy=0. |
| 6 | Solve $(x^2y+2xy^2)dx-(x^3-3x^2y)dy=0.$ |
| 7 | Solve $\cos^2 x \frac{dy}{dx} + y = \tan x$. |
| 8 | Solve $\frac{dy}{dx} + \frac{2}{x}y = 3x^2 y^{3 4}$. |
| 9 | Solve $\frac{d^3y}{dx^3} - 3\frac{d^2y}{dx^2} + 4y = 0$ |
| 10 | $\frac{d^3y}{dx^3} + 2\frac{d^2y}{dx^2} + \frac{dy}{dx} = e^{2x} + x^2 + x.$ |
| 11 | Solve $\frac{d^2y}{dx^2} - \frac{dy}{dx} + 4y = e^x \cos x + \sin 2x$. |
| 12 | Find the orthogonal trajectories of the system of curves $r^n sinn \theta = a^n$ |
| 13 | Using method of variation of parameter solve i) 6 y" +5y' -6y =x. |
| | ii) y'' +y = $2\sin x \cdot \sin 2x$. |
| 14 | Solve $x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} + y = 2 \log x$ |
| 15 | Solve $x^{2}\frac{d^{2}y}{dx^{2}} + 2x\frac{dy}{dx} - 20y = (x + 1)^{2}$ |
| 16 | Solve $(5+2x)^2 \frac{d^2y}{dx^2} - 6(5+2x)\frac{dy}{dx} + 8y = 0$ |
| 17 | Show that the system of parabolas $y^2 = 4a(x+a)$ is self-orthogonal. |
| 18 | Solve $(2x - 1)^3 \frac{d^3y}{dx^3} + (2x - 1)\frac{dy}{dx} - 2y = 0$ |
| 19 | Solve $x \frac{d^2y}{dx^2} + (1-x)\frac{dy}{dx} - y = e^x$ |
| 20 | Solve $3x^2 \frac{d^2y}{dx^2} + (2x - 6x^2)\frac{dy}{dx} - 4y = 0$ |
| 21 | i) solve $\frac{dx}{dt} - 7x + y = 0$, $\frac{dy}{dt} - 2x - 5y = 0$ ii) Solve $\frac{dx}{x^2 - y^2 - z^2} = \frac{dy}{2xy} = \frac{dz}{2xz}$ |
| 22 | i) Solve $(y + z)dz + dy + dz = 0$ |
| | ii) Solve $\frac{adx}{(b-c)xy} = \frac{bdy}{(c-a)zx} = \frac{cdz}{(a-b)xy}$ |
| 23 | i) Solve $(y + z)dx + (2 + x)dy + (x + y)dz = 0$ ii) solve $\frac{dx}{dx} + 4x + 3y - t$ $\frac{dy}{dx} + 2x + 5y - e^{t}$ |
| | $\frac{dt}{dt} = \frac{1}{t} + $ |
| 24 | Verify that the function ϕ_1 satisfies the equation, and find a second independent solution |
| | $x^2y'' - 7xy' + 15y = 0, \varphi_1(x) = x^3.$ |

- Daniel A. Murray, "Introductory Course in Differential Equations", Universities Press
- 2. G. F. Simmons "Differential Equations with Applications and Historical Notes", Second Edition, Mc Graw Hill.
- 3. M.D. Raisinghania, "Ordinary and Partial Differential Equations", S Chand and Company Ltd
- 4. T M Karade, "Differential Equation", Sonu –Nilu Publication





(Autonomous) Department of Mathematics

Course Type : DSC-VIIICourse Title : Ring TheoryCourse Code : 201MAT4102Credits : 03

Max. Marks: 75

Lectures: 45 Hrs.

Learning Objectives

- LO1 Definition and some classes of Rings
- LO2 Ideals, Quotient ring.
- LO3 Euclidean rings and their properties.
- LO4 Polynomial Ring
- LO5 Reducibility and irreducibility of polynomial

Course outcomes

- CO1 Analyze classes of rings
- CO2 Find quotient structure of quotient ring
- CO3 Learn Euclidean ring and examples.
- CO4 Evaluate reducibility and irreducibility of polynomials

| Unit | Title of Unit & Contents | Hrs | |
|------|---|------|--|
| NO. | Pinge | . 10 | |
| 1 | Definition and examples of rings | 10 | |
| | Some special classes of rings | | |
| | Subring and Characteristic of ring | | |
| | Unit Outcome: | | |
| | UO1 Classify the various rings with terminology | | |
| | UO2 Identify Characteristic of Rings | | |
| II | Ideals and quotients rings | 12 | |
| | Ideals and quotients rings | | |
| | More ideals and quotients rings | | |
| | The field of quotients of an integral domains . | | |
| | Unit Outcome: | | |
| | UO1 Get knowledge of ideals and quotient ring | | |
| | UO2 Find quotient structure of quotient ring. | | |
| III | Homomorphism | 10 | |
| | Homomorphism of rings | | |
| | Isomorphism | | |
| | Fundamental theorem of homomorphism | | |
| | Kernels of Homomorphism | | |

| Unit No. | Title of Unit & Contents | | | | | | | | |
|-------------|--|--|--|--|--|--|--|--|--|
| | Unit Outcomes | | | | | | | | |
| | UO1 Get concept of homomorphism | | | | | | | | |
| | UO2 Find Kernel of homomorphism | | | | | | | | |
| IV | Euclidean ring and Polynomial ring | | | | | | | | |
| | Euclidean rings | | | | | | | | |
| | A particular Euclidean ring (Ring of Gaussian Integers) | | | | | | | | |
| | Unique Factorization theorem | | | | | | | | |
| | Polynomial rings | | | | | | | | |
| | Polynomial oven the rational fields. | | | | | | | | |
| | Unit Outcome: | | | | | | | | |
| | UO1 Learn Euclidean ring and examples . | | | | | | | | |
| | UO2 Learn Properties of polynomials | | | | | | | | |
| | UO3 Evaluate reducibility and irreducibility of polynomials. | | | | | | | | |

- 1. Topics in Algebra, I.N. Herstein, John Wiley and Sons (New York)
- 2. A first course in abstract algebra, by J.B. Fraleigh, Narosa Publications.
- 3. Contemparary Abstract Algebra, by Joseph Gallion, Narosa Publications.
- 4. Modern Algebra, by A.<mark>R. Vas</mark>ishtha, Krishna Prakashan Media
- 5. Modern Algebra, by R.P. Rohtatgi, Dominant Publishers and Distributors, New Delhi.
- 6. Modern Algebra, By Goyal and Gupta, Pragato Prakashan Meerut
- 7. College Mathematics, by N.R. Jayaram and R.V. Prabhakara, Himalaya Publishing House.
- 8. Elements of Logic and Modern Algebra, by M.V. Bhat and M.L. Bhave, S. Chand and Company Ltd. Ramnagar, New Delhi 110055
- 9. Lectures on Abstract Agebra By T M Karade J N Salunke ,K S Adhav, Maya Bendre, Sonu Nilu Publication



(Autonomous) Department of Mathematics

Course Type : Lab-Course –VIIICourse Title : Lab-Course (Based on DSC-VIII)Course Code : 201MAT4104Credits : 01Max. Marks: 50

Lectures: 30 Hrs.

Learning Objectives

- LO1 Definition and some classes of Rings
- LO2 Ideals, Quotient ring.
- LO3 Euclidean rings and their properties.
- LO4 Polynomial Ring
- LO5 Reducibility and irreducibility of polynomial

Course outcomes

- CO1 Analyze classes of rings
- CO2 Find quotient structure of quotient ring
- CO3 Learn Euclidean ring and examples.
- CO4 Evaluate reducibility and irreducibility of polynomials

| Practical No. | Unit |
|---------------|---|
| 1 | Prove that if R is Ring and $a, b \in R$, then $(a + b)^2 = a^2 + ab + ba + b^2$, where by x^2 we mean xx |
| 2 | If every if $x \in R$, satisfies $x^2 = x$, prove that R must be commutative (A ring in which $x^2 = x$ for all elements is called a Boolean Ring.) |
| 3 | If D is an integral domain and D is of finite Characteristics, prove that the characteristics of D is a prime number. |
| 4 | If D is an integral Domain and if na=0 for some $a \neq 0$ in D and some integer $n \neq 0$, prove that D is of finite characteristics |
| 5 | If R is system satisfying all the conditions for a ring with unit element with the possible exception of $a + b = b + a$, prove that the axiom $a + b = b + a$ must hold in R is thus a Ring. |
| 6 | Show that the commutative ring D is an integral domain iff for a, b, c , $\epsilon Da \neq 0$ the relation $ab = ac$ implies that $b = c$. |
| 7 | If U is an ideal of R and $1 \in U$, prove that U=R. |
| 8 | If F is a field, prove that's its only ideal is (0) and f itself |
| 9 | If R is Commutative ring and $a, \in R$,a.Show that $aR = \{ar r \in R\}$ is a two sided ideal of R |

| Practical No. | Unit | | | | | | | | |
|---------------|--|--|--|--|--|--|--|--|--|
| | b. Show by an example that this may be false if R is not Commutative | | | | | | | | |
| 10 | If U, V are ideals of R, let $U + V = \{u + v u \in U, v \in V\}$. Prove that $U + V$ is also an ideal. | | | | | | | | |
| 11 | If U is an ideal of R, let $r(U) = \{x \in R xu = 0 \text{ for all } u \in U\}$ prove that $r(U)$ is an ideal of R. | | | | | | | | |
| 12 | Let R be a Ring with unit element, R not necessarily commutative, such that the only right- ideals of R are (0) and R. prove that R is a Division Ring. | | | | | | | | |
| 13 | Let J be a ring of integ <mark>ers, p</mark> a prime number, and (p) the ideal of J consisting of all multi <mark>ples of</mark> p. prove | | | | | | | | |
| | a. $J (p)$ is isomorphic to J_p , the ring of integer modulo p b. J_p is an field. | | | | | | | | |
| 14 | Let R be the ring of all real-valued continuous functions on the closed unit interval. If M is a Maximal ideal of R, prove that there exists a real number γ , $0 \le \gamma \le 1$, such that $M = M_{\gamma} = \{f(x) \in R f(\gamma) = 0\}$. | | | | | | | | |
| 15 | Let $J(\sqrt{2})$ be all real number of the form $m + n\sqrt{2}$, where m, n are integers; Prove that $J(\sqrt{2})$ forms a ring under the usual addition and multiplication of real numbers. Define $\emptyset: J(\sqrt{2}) \to J(\sqrt{2})$ by $\emptyset(m + n\sqrt{2}) = m - n\sqrt{2}$. Verify that \emptyset is Homomorphism of $J(\sqrt{2})$ onto $J(\sqrt{2})$ and its kernel $I(\emptyset)$, consists only of 0. | | | | | | | | |
| 16 | Prove that the mapping $\emptyset: D \to F$ defined by $\emptyset(a) = [a, 1]$ is an isomorphism of D into F. | | | | | | | | |
| 17 | Find all the units in <i>J</i> [<i>i</i>],F[X] | | | | | | | | |
| 18 | If $a + bi$ is not a unit of $J[i]$ prove that $a^2 + b^2 > 1$. | | | | | | | | |
| 19 | Find the Greatest common divisor of the following polynomials over F, the field of rational numbers: a. $x^3 - 6x^2 + x + 4$ and $x^5 - 6x + 1$ b. $x^2 + 1$ and $x^6 + x^3 + x + 1$ | | | | | | | | |
| 20 | Prove that:a. $x^2 + x + 1$ is irreducible over F, the field of integers mod 2.b. $x^2 + 1$ is irreducible over F, the integers mod 7.c. $x^3 - 9$ is irreducible over F, the integers mod 91.d. $x^3 - 9$ is irreducible over the integers mod 11. | | | | | | | | |
| 21 | Prove that $x^2 + 1$ is irreducible over the field F of integers mod 11 and prove directly that $F[x]/(x^2 + 1)$ is a field having 121 elements. | | | | | | | | |
| 22 | Let F be the field of real numbers. Prove that $F[x]/(x^2 + 1)$ is a field isomorphic to the field of complex numbers. | | | | | | | | |

| Practical No. | Unit |
|---------------|---|
| 23 | If p is prime number, prove that the polynomial $x^n - p$ is irreducible over the rationals. |
| 24 | If a is rational and $x - a$ divides an integers monic polynomial, prove that the a must be an integer. |

- 1. Topics in Algebra, I.N. Herstein, John Wiley and Sons (New York)
- 2. A first course in abstract algebra, by J.B. Fraleigh, Narosa Publications.
- 3. Contemparary Abstract Algebra, by Joseph Gallion, Narosa Publications.
- 4. Modern Algebra, by A.R. Vasishtha, Krishna Prakashan Media
- 5. Modern Algebra, by R.P. Rohtatg<mark>i, Dominant Publishers and Distributors, New Delhi.</mark>
- 6. Modern Algebra, By Goyal and G<mark>upta, Pragat</mark>o Prakashan Meerut
- 7. College Mathematics, by N.R. Jayaram and R.V. Prabhakara, Himalaya Publishing House.
- 8. Elements of Logic and Modern Algebra, by M.V. Bhat and M.L. Bhave, S. Chand and Company Ltd. Ramnagar, New Delhi 110055
- 9. Lectures on Abstract Algebra by T M Karade J N Salunke, K S Adhav, Maya Bendre, Sonu Nilu Publication





(Autonomous) Department of Mathematics

Course Type : DSM-IICourse Title : Fundamentals of StatisticsCourse Code : 201MAT4301Credits : 03Max. Marks: 75Lectures: 45 Hrs.

Learning Objectives:

- LO1 To identify the various approaches to inferential statistics and their strengths and weaknesses
- LO2 To display data graphically and interpret graphs: stem plots, histograms, and box plots
- LO3 To recognize, describe, and calculate the measures of the spread of data: variance, standard deviation, and range
- LO4 To understand and use the terminology of probability

Course Outcomes:

- CO1 Create and interpret frequency tables
- CO2 Calculate the measures of the center of data: mean, median, and mode
- CO3 Calculate the measures of location of data: quartiles and percentiles
- CO4 Calculate probabilities using the Addition Rules and Multiplication Rules

| Unit No. | Title of Unit & Contents | | | | | | | | | |
|-------------|------------------------------|---|--|--|--|--|--|--|--|--|
| Ι | Frequency Distribution | | | | | | | | | |
| | 1. | Frequency Distr <mark>ibutio</mark> n, Continuous Frequency Distribution, | | | | | | | | |
| | | Graphic Representation of a Frequency Distribution | | | | | | | | |
| | 2. | Histogram | | | | | | | | |
| | 3. | Frequency Polygon | | | | | | | | |
| | Unit | Outcome: | | | | | | | | |
| | U01 | 1 To understand frequency distribution and its types | | | | | | | | |
| | U02 | 02 To draw Histogram and frequency polygon | | | | | | | | |
| II | Measures of Central Tendency | | | | | | | | | |
| | 1. | Arithmetic Mean, Properties of Arithmetic Mean, Geometric | | | | | | | | |
| | | Mean, Harmonic Mean | | | | | | | | |
| | 2. Weighted Mean | | | | | | | | | |
| | 3. | Median | | | | | | | | |
| | 4. | Mode | | | | | | | | |
| | Unit Outcome: | | | | | | | | | |
| | U01 | Calculate Mean, Median and Mode for the grouped and | | | | | | | | |
| | | ungrouped data | | | | | | | | |

| Unit No. | Title of Unit & Contents | | | | | | | | |
|-------------|---|--|--|--|--|--|--|--|--|
| III | Measures of Dispersion | | | | | | | | |
| | 1. Measures of dispersion –range, quartile deviation | | | | | | | | |
| | 2. Mean Deviation for grouped and ungrouped data | | | | | | | | |
| | 3. Variance and Standard Deviation | | | | | | | | |
| | 4. Analysis of Frequency Distribution | | | | | | | | |
| | Unit Outcome: | | | | | | | | |
| | Calculate range,QD,MD,SD for the frequency distribution | | | | | | | | |
| IV | Probability | | | | | | | | |
| | 1. Random Experiments; Event | | | | | | | | |
| | 2. Axiomatic Approach to Probability | | | | | | | | |
| | 3. Conditional Probability and its properties | | | | | | | | |
| | 4. Multiplication Theorem on Probability; Independent Events; | | | | | | | | |
| | Bayes' Theorem | | | | | | | | |
| | Unit Outcome: | | | | | | | | |
| | UO1 Understand Sampl <mark>e space, E</mark> vents, probability of a random | | | | | | | | |
| | experiment. | | | | | | | | |

- 1. S.C. Gupta and V.K. Kapoor, "Fundamentals of Mathematical Statistics (A Modern Approach), Tenth Revised Edition, Sultan Chand & Sons Educational Publishers New Delhi.
- 2. S. Saha, "Basic Business Mathematics and Statistics", New Central Book Agency, (P), Ltd, Calcutta.





Rajarshi Shahu Mahavidyalaya, Latur

(Autonomous) Department of Mathematics

Course Type : Lab-Course IICourse Title : Lab-Course (Based on DSM-II)Course Code : 201MAT4302Credits : 01Max. Marks: 50

Lectures: 30 Hrs.

Learning Objectives:

- LO1 To identify the various approaches to inferential statistics and their strengths and weaknesses
- LO2 To display data graphically and interpret graphs: stem plots, histograms, and box plots
- LO3 To recognize, describe, and calculate the measures of the spread of data: variance, standard deviation, and range
- LO4 To understand and use the terminology of probability

Course Outcomes:

- CO1 Create and interpret frequency tables
- CO2 Calculate the measures of the center of data: mean, median, and mode
- CO3 Calculate the measures of location of data: quartiles and percentiles
- CO4 Calculate probabilities using the Addition Rules and Multiplication Rules

| Practical No. | Practical's | | | | | | |
|---------------|--|--|--|--|--|--|--|
| 1 | Problems on frequency distribution | | | | | | |
| 2 | Problems on continuous frequency distribution | | | | | | |
| 3 | Problems on graphic representation of a frequency distribution | | | | | | |
| 4 | Problems on Histogram | | | | | | |
| 5 | Problems on Frequency Polygon | | | | | | |
| 6 | Problems on Arithmetic Mean | | | | | | |
| 7 | Problems on Properties of Arithmetic Mean | | | | | | |
| 8 | Problems on Geometric Mean and a second seco | | | | | | |
| 9 | Problems on Harmonic Mean | | | | | | |
| 10 | Problems on Weighted Mean | | | | | | |
| 11 | Problems on Median | | | | | | |
| 12 | Problems on Mode | | | | | | |
| 13 | Problems on Measures of dispersion –range, quartile deviation | | | | | | |
| 14 | Problems on mean deviation for grouped and ungrouped data | | | | | | |

| Practical No. | Practical's |
|---------------|--|
| 15 | Problems on variance and standard deviation |
| 16 | Problems on frequency distribution |
| 17 | Problems on Random Experiments and event |
| 18 | Problems on probability |
| 19 | Problems on conditional Probability |
| 20 | Problems on Independent events; Bayes' theorem |

- 1. S.C. Gupta and V.K. Kapoor, "Fundamentals of Mathematical Statistics (A Modern Approach), Tenth Revised Edition, Sultan Chand & Sons Educational Publishers New Delhi.
- 2. S. Saha, "Basic Business Mathematics and Statistics", New Central Book Agency, (P), Ltd, Calcutta.





(Autonomous)

UG First Year

Extra Credit Activities

| Sr. | Course Title | Course Title Credits | | | |
|-----|-----------------------------|-----------------------|-----------------|--|--|
| No. | | | T/P | | |
| 1 | MOOCs | Min. of 02 credits | Min. of 30 Hrs. | | |
| 2 | Certificate Courses | Min. of 02 credits | Min. of 30 Hrs. | | |
| 3 | IIT Spoken Tutorial Courses | Min. of 02 credits | Min. of 30 Hrs. | | |

Guidelines:

Extra -academic activities

- 1. All extra credits claimed under this heading will require sufficient academic input/ contribution from the students concerned.
- 2. Maximum 04 extra credits in each academic year will be allotted.
- 3. These extra academic activity credits will not be considered for calculation of SGPA/CGPA but will be indicated on the grade card.

Additional Credits for Online Courses:

- 1. Courses only from SWAYAM and NPTEL platform are eligible for claiming credits.
- 2. Students should get the consent from the concerned subject Teacher/Mentor/Vice Principal and Principal prior to starting of the course.
- 3. Students who complete such online courses for additional credits will be examined/verified by the concerned mentor/internal faculty member before awarding credits.
- 4. Credit allotted to the course by SWAYAM and NPTEL platform will be considered as it is.

Additional Credits for Other Academic Activities:

- 1. One credit for presentation and publication of paper in International/National/State level seminars/workshops.
- One credit for measurable research work undertaken and field trips amounting to 30 hours of recorded work.
- 3. One credit for creating models in sponsored exhibitions/other exhibits, which are approved by the concerned department.
- 4. One credit for any voluntary social service/Nation building exercise which is in collaboration with the outreach center, equivalent to 30 hours
- 5. All these credits must be approved by the College Committee.

Additional Credits for Certificate Courses:

- 1. Students can get additional credits (number of credits will depend on the course duration) from certificate courses offered by the college.
- 2. The student must successfully complete the course. These credits must be approved by the Course Coordinators.
- Students who undertake summer projects/ internships/ training in institutions of repute through a national selection process, will get 2 credits for each such activity. This must be done under the supervision of the concerned faculty/mentor.

Note:

- 1. The respective documents should be submitted within 10 days after completion of Semester End Examination.
- 2. No credits can be granted for organizing or for serving as office bearers/volunteers for Inter-Class / Associations / Sports / Social Service activities.
- 3. The office bearers and volunteers may be given a letter of appreciation by the respective staff coordinators. Besides, no credits can be claimed for any services/ activities conducted or attended within the college.
- 4. All claims for the credits by the students should be made and approved by the mentor in the same academic year of completing the activity.
- 5. Any grievances of denial/rejection of credits should be addressed to Additional Credits Coordinator in the same academic year.

6. Students having a shortage of additional credits at the end of the third year can meet the Additional Credits Coordinator, who will provide the right advice on the activities that can help them earn credits required for graduation.



शिव छत्रपती

क्षिण संस्था



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Examination Framework

Theory:

40% Continuous Assessment Tests (CATs) and 60% Semester End Examination (SEE)

Practical:

50% Continuous Assessment Tests (CATs) and 50% Semester End Examination (SEE)

| Course | Marks | CAT & Mid Term Theory | | | | CAT Practical | | Best Scored CAT & Mid Term | SEE | Total |
|-------------------------------|-------|--------------------------|-------|-------------|-----------|------------------|-----|--|-----|-------|
| | | 3 | | | 4 | | | | | |
| 1 | 2 | Att. | CAT I | Mid Term | CAT II | Att. | САТ | 5 | 6 | 5 + 6 |
| DSC/DSE/OE/ Minor | 100 | 10 | 10 | 20 | 10 | - | - | 40 | 60 | 100 |
| DSC | 75 | 05 | 10 | 15 | 10 | - | - | 30 | 45 | 75 |
| Lab Course/AIPC/ OJT/FP | 50 | | - | - | - | 05 | 20 | - | 25 | 50 |
| VSC/SEC/ AEC/VEC/CC | 50 | 05 | 05 | 10 | 05 | - | - | 20 | 30 | 50 |

Note:

शिव छत्रपती शिक्षण संस्था

- 1. All Internal Exams are compulsory
- 2. Out of 02 CATs best score will be considered
- 3. Mid Term Exam will be conducted by the Exam Section
- 4. Mid Term Exam is of Objective nature (MCQ)
- 5. Semester End Exam is of descriptive in nature (Long & Short Answer)
- 6. CAT Practical (20 Marks): Lab Journal (Record Book) 10 Marks, Overall Performance 10 Marks.

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